

- 1 (a) (i)  $MB = \sqrt{(DB)^2 - (DM)^2}$   
 $= \sqrt{72^2 - 43^2}$   
 $= \sqrt{3335}$   
 $= 57.749$   
 $\approx 57.7$  m
- (ii)  $AB = AM + MB$   
 $= 57.749 + \frac{43}{\tan 62^\circ}$   
 $= 80.613$   
 $\approx 80.6$  m
- (iii)  $CD = \frac{72}{\sin 23^\circ}$   
 $= 184.27$   
 $\approx 184$  m
- (b)  $M\hat{B}D = \sin^{-1} \frac{43}{72}$   
 $= 36.671^\circ$   
 Bearing of  $D$  from  $B = 270^\circ - 36.671^\circ$   
 $= 233.329^\circ$   
 $\approx 233.3^\circ$

- 2 (a)  $\frac{x}{8} = \frac{50}{x}$   
 $x^2 = 8 \times 50 = 400$   
 $x = \pm \sqrt{400}$   
 $= \pm 20$
- (b)  $\frac{t+p}{4} = \frac{q}{5}$   
 $t+p = \frac{4q}{5}$   
 $t = \frac{4q}{5} - p$   
 $\therefore t = \frac{4q-5p}{5}$
- (c) (i)  $y = a + \frac{600}{x}$   
 $17 = a + \frac{600}{50}$   
 $\therefore a = 17 - 12 = 5$
- (ii)  $y = 5 + \frac{600}{x}$   
 $= 5 + \frac{600}{100}$   
 $= \$11$

(iii) Total cost  $= 300 \left( 5 + \frac{600}{300} \right)$   
 $= 300(5 + 2)$   
 $= \$2100$

(iv)  $y = 5 + \frac{600}{x}$   
 $5.2 = 5 + \frac{600}{x}$   
 $0.2 = \frac{600}{x}$   
 $x = \frac{600}{0.2} = 3000$  copies

- 3 (a) (i) Total amount  $= 1299 \times \frac{1}{3} + 24 \times 40.30$   
 $= \$1400.20$
- (ii)  $\frac{1400.20 - 1299}{1299} \times 100\% = 7 \frac{1027}{1299}\%$   
 $\approx 7.79\%$

(b)  $1299(1.06^3 - 1) = \$248.13$

(c)  $759 \times \frac{100}{115} = \$660$

- 4 (a)  $y - y_1 = m(x - x_1)$   
 $y - 4 = \frac{4}{3}(x - (-5))$   
 $3y = 4x + 4(5) + 3(4)$   
 $3y = 4x + 32$

The equation of line  $AB$  is  $3y = 4x + 32$ .

- (b)  $2x + 9y = 68$   
 $2x = 68 - 9y$   
 $4x = 136 - 18y$

Substitute this equation into  $3y = 4x + 32$ .

$$3y = 136 - 18y + 32$$

$$21y = 168$$

$$y = 8$$

$$x = \frac{68 - 9(8)}{2} = -2$$

The coordinates of  $B$  is  $(-2, 8)$ .

(c) (i)  $|\overline{AE}| = \sqrt{6^2 + 1^2} = \sqrt{37} \approx 6.08$

(ii)  $E(-5+6, 4+1) \Rightarrow E(1, 5)$

(iii)  $\overline{DE} = \overline{OE} - \overline{OD} = \begin{pmatrix} 1 \\ 5 \end{pmatrix} - \begin{pmatrix} 4 \\ 2 \end{pmatrix} = \begin{pmatrix} -3 \\ 3 \end{pmatrix}$

$$\overline{DB} = \overline{OB} - \overline{OD} = \begin{pmatrix} -2 \\ 8 \end{pmatrix} - \begin{pmatrix} 4 \\ 2 \end{pmatrix} = \begin{pmatrix} -6 \\ 6 \end{pmatrix}$$

- (iv) 1.  $D, E$  and  $B$  are collinear since there is a common vector  $\begin{pmatrix} -1 \\ 1 \end{pmatrix}$ .

2.  $E$  is exactly midway between  $B$  and  $D$  since  $\overline{DB} = 2\overline{DE}$ .

- 5 (a) (i)  $\hat{XCD} = \frac{360^\circ}{15} = 24^\circ$   
(ii)  $\hat{CXD} = 180^\circ - 2(24^\circ) = 132^\circ$   
(b) Since  $\hat{XDC} = 24^\circ$ , triangle  $XCD$  is isosceles.  
 $\Rightarrow XC = XD$   
Given  $BC = DE$ ,  
 $XB = XC + BC = XD + DE = XE$   
(c)  $\hat{BED} = \hat{CDX} = 24^\circ$   
Let  $Y$  denote a point on  $FE$  extended.  
 $\hat{DEY} = 24^\circ$  (exterior angle)  
 $\hat{BEF} = 180^\circ - 24^\circ - 24^\circ = 132^\circ$

- 6 (a) Number of hours taken =  $\frac{42}{x}$   
(b) Number of hours taken =  $\frac{42}{x - \frac{1}{2}}$   
(c)  $\frac{42}{x - \frac{1}{2}} - \frac{42}{x} = \frac{10}{60}$   
 $6\left[42x - 42\left(x - \frac{1}{2}\right)\right] = x\left(x - \frac{1}{2}\right)$   
 $252x - 252x + 126 = x^2 - \frac{x}{2}$   
 $2x^2 - x - 252 = 0$   
(d)  $2x^2 - x - 252 = 0$   
 $x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(2)(-252)}}{2(2)}$   
 $x = 11.478$  OR  $x = -10.978$   
(e) Since  $x$  is positive, let  $x = 11.478$ .  
Time taken =  $\frac{42}{11.478}$   
= 3.659 hours  
 $\approx 3$  h 39 min 33 s

- 7 (a)  $170^2 = 95^2 + 102^2 - 2(95)(102) \cos \hat{PQR}$   
 $\hat{PQR} = \cos^{-1} \left( \frac{170^2 - 95^2 - 102^2}{-2(95)(102)} \right)$   
=  $119.255^\circ$   
 $\approx 119.3^\circ$   
(b) Angle of depression of  $Q$  from  $B$   
=  $\tan^{-1} \frac{23}{95}$   
=  $13.6097^\circ$   
 $\approx 13.6^\circ$   
(c)  $\frac{1}{2}(170)(RS) \sin 52^\circ = 5200$   
 $RS = \frac{2(5200)}{170 \sin 52^\circ}$   
= 77.634  
 $\approx 77.6$  m

- (d) (i)  $77.634 \div 3 = 25.878$   
 $\therefore 26$  panels need to be bought  
(ii) Number of posts required  
=  $26 + 1$   
= 27  
Total cost =  $26(28.50) + 27(14.95)$   
= \$1144.65

- 8 (a) (i)  $PRQ = 44 - 2(8) = 28$   
From  $s = r\theta$ ,  
 $28 = 8\theta$   
 $\theta = 3\frac{1}{2}$   
(ii)  $\hat{POQ} = 2\pi - 3\frac{1}{2}$   
Area of triangle  $POQ$   
=  $\frac{1}{2}(8)(8) \sin \hat{POQ}$   
= 11.225  
 $\approx 11.2$  m<sup>2</sup>  
(iii) Total area =  $11.225 + \frac{1}{2}r^2\theta$   
=  $11.225 + \frac{1}{2}(8^2)(3.5)$   
=  $11.225 + 112$   
 $\approx 123$  m<sup>2</sup>  
(b) (i) Total volume  
= Volume of pyramid  
+ Volume of cuboid  
=  $\frac{1}{3} \times 10 \times 10 \times 12 + 30 \times 10 \times 10$   
=  $3400$  cm<sup>3</sup>  
(ii) Let  $M$  denote the midpoint of  $AB$ .  
 $MN = 10 \div 2 = 5$   
 $VM = \sqrt{(MN)^2 + (VN)^2}$   
=  $\sqrt{5^2 + 12^2}$   
= 13  
Area of triangle  $VAB = \frac{1}{2} \times 10 \times 13$   
=  $65$  cm<sup>2</sup>  
Total area =  $4(65) + 4(30 \times 10)$   
=  $1460$  cm<sup>2</sup>
- 9 (a) See graph below  
(b) (i)  $m = 5.15$   
(ii)  $t = 17$   
(iii)  $t = 31$   
(c) (i) Gradient =  $\frac{3.55 - 2.20}{-10 - 40}$   
=  $\frac{1.35}{-50}$   
=  $-0.027$

(ii) The gradient represents the rate of change of mass at the particular instant. When  $t = 7$ , the mass is decreasing at  $-0.027$  kg/day instantaneously.

(d) The relationship between  $m$  and  $t$  may be different for values of  $t$  beyond the given range. In this case,  $t = 365 > 70$ .

10 (a) (i)  $a = 28 \div 4 = 7$   
 $b = 60 - (12 + 15 + 10 + 7 + 4 + 0 + 2 + 1) = 9$   
 $c = 12 \times 0 = 0$   
 $d = 3 \times 9 = 27$   
 $e = 0 + 15 + 20 + 27 + 28 + 20 + 0 + 14 + 8$   
 $= 132$

(ii) Mean =  $\frac{\sum fx}{\sum f} = \frac{132}{60} = 2\frac{1}{5}$

Standard deviation =  $\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$   
 $= \sqrt{\frac{510}{60} - \left(2\frac{1}{5}\right)^2}$   
 $= \sqrt{\frac{183}{50}}$   
 $= 1.91$

(b) Probability = 0

(c) Number of pupils who had read more than 4 books  
 $= 4 + 2 + 1 = 7$

P(both had read more than 4 books)  
 $= \frac{7}{60} \times \frac{6}{59} = \frac{7}{590}$

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9 (a)

